Closure and commutability results for Γ -limits

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Under a suitable notion of equivalence of integral densities we prove a Γ -closure theorem for integral functionals with standard *p*-growth: The limit of a sequence of Γ convergent families is again a Γ -convergent family. Its Γ -limit can be recovered from Γ -limits of the original problems. This result not only provides a common basic principle for a number of linearization and homogenization results in elasticity theory. It also allows for new applications as we exemplify by proving that geometric linearization and homogenization of multi-well energy functionals commute. We then also address the case p = 1 with its difficulties.

Schematically:

$$\begin{array}{cccc} \mathcal{F}_{\varepsilon}^{(j)} & \approx & \mathcal{F}_{\varepsilon}^{(\infty)} \\ & & & & \\ & & & \uparrow \\ \mathcal{F}_{0}^{(j)} & \xrightarrow{?} & \mathcal{F}_{0}^{(\infty)} \end{array}$$

The poster is based on joint work with Bernd Schmidt (Augsburg University).

References:

 M. Jesenko, B. Schmidt: Closure and commutability results for Γ-limits and the geometric linearization and homogenization of multiwell energy functionals. SIAM J. Math. Anal. 46 (2014), no. 4, 2525–2553.