



Simulation of Synchronous-Hysteresis Superconducting Machine

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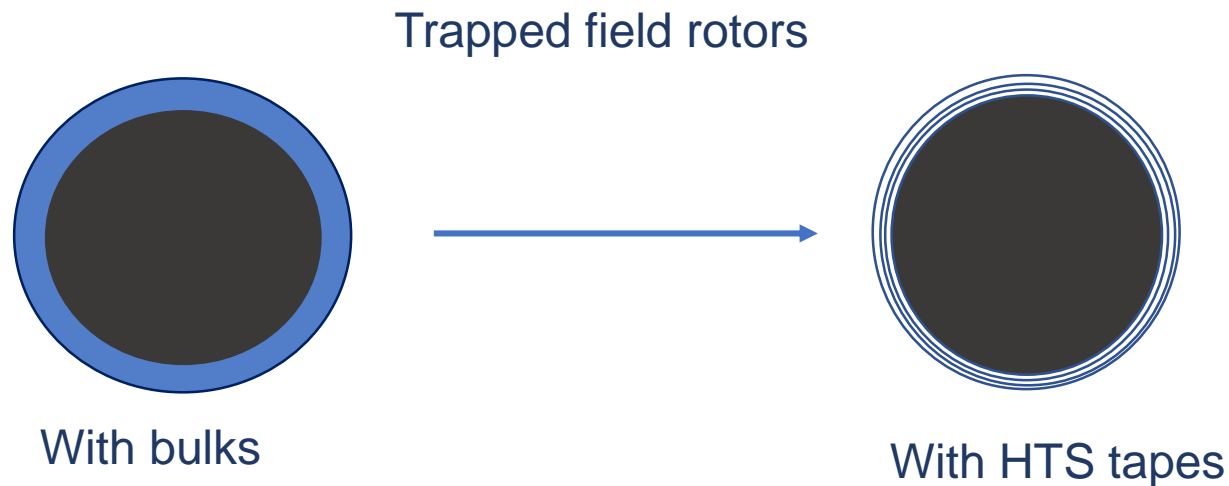


Outline

1. Motivation
2. Studied prototype
3. Objectives
4. Simulation Models
5. Results
6. Conclusion

Motivation

- Several works in the literature have proposed replacing HTS bulks by HTS 2G tapes in trapped field motors*



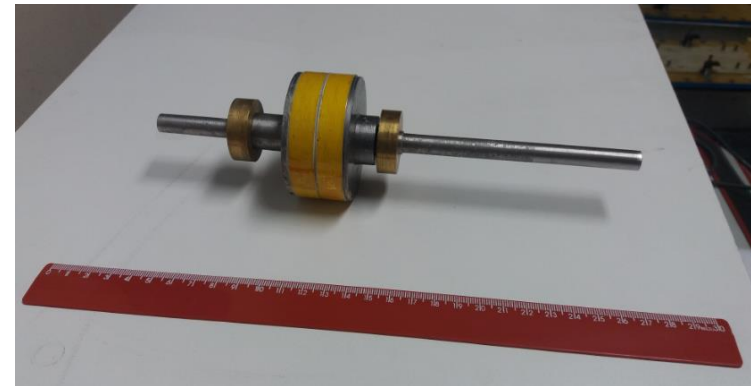
*G.G. Sotelo, F. Sass, M. Carrera, J. Lopez-Lopez and X. Granados. Proposal of a Novel Design for Linear Superconducting Motor Using 2G Tape Stack. *IEEE Transactions on Industrial Electronics.*, vol 65, no 9, Sept. 2018.

Studied Prototype

Prototype built at UFRJ and CEPEL. Non-superconducting three-phase stator and rotor made of two rings of **nine turns of HTS 2G tapes** wrapped around a ferromagnetic cylinder.



Adapted from a 0.47Nm
Permanent Magnet Machine

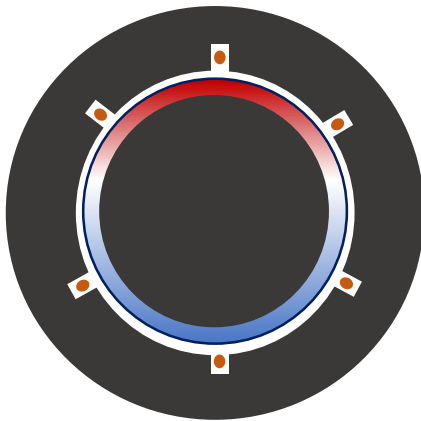


Maximum radius	56 mm
Length	28 mm
Tape	SuperPower SF12050
Phases and Poles	3 Phases, 6 Poles
Critical current measured	377 A

Studied Prototype

Trapped Field Motor with HTS 2G Tapes

Superconductor is magnetized by the rotating magnetic field applied



The mode of operation depends on the mechanical torque

$$\tau_{mec} < \tau_{pinning} \longrightarrow \omega_{mec} = \omega_{sinc}$$

Synchronous machine

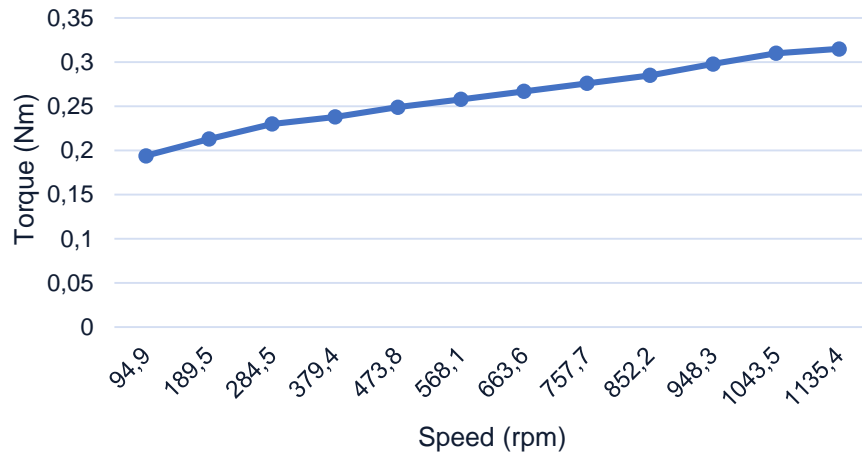
$$\tau_{mec} > \tau_{pinning} \longrightarrow \omega_{mec} < \omega_{sinc}$$

Hysteresis machine

Studied Prototype

Experimental data

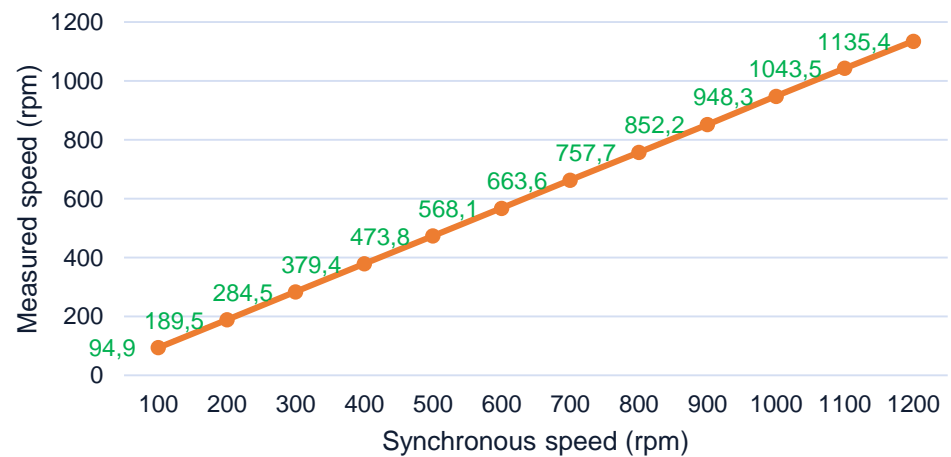
Torque vs Speed



Mechanical torque applied.

5% slip appeared in the torque vs speed curve

Measured speed vs Synchronous speed



Objectives

- Observe the induced current density in the rings at locked rotor → **H Formulation**
- Analyse machine behavior at synchronous speed → **A-V Formulation**
- Analyse the dynamic response → **Mixed A-V-H Formulation**

Simulation Models

Simulation Models: H Formulation

COMSOL's Magnetic Field Formulation

$$\nabla \times \mathbf{H} = \mathbf{J}$$

$$\frac{\mu \partial \mathbf{H}}{\partial t} + \nabla \times \mathbf{E} = 0$$

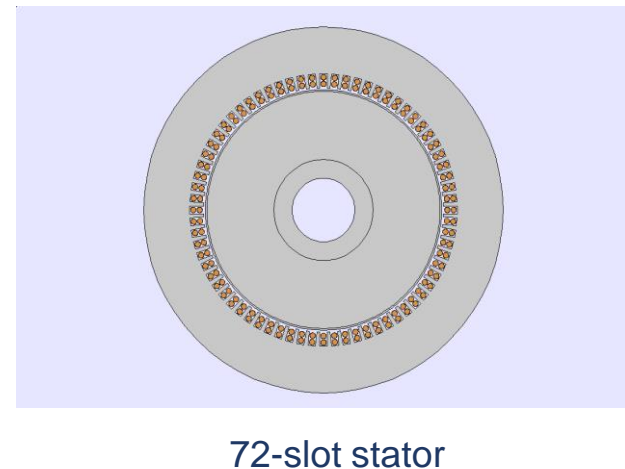
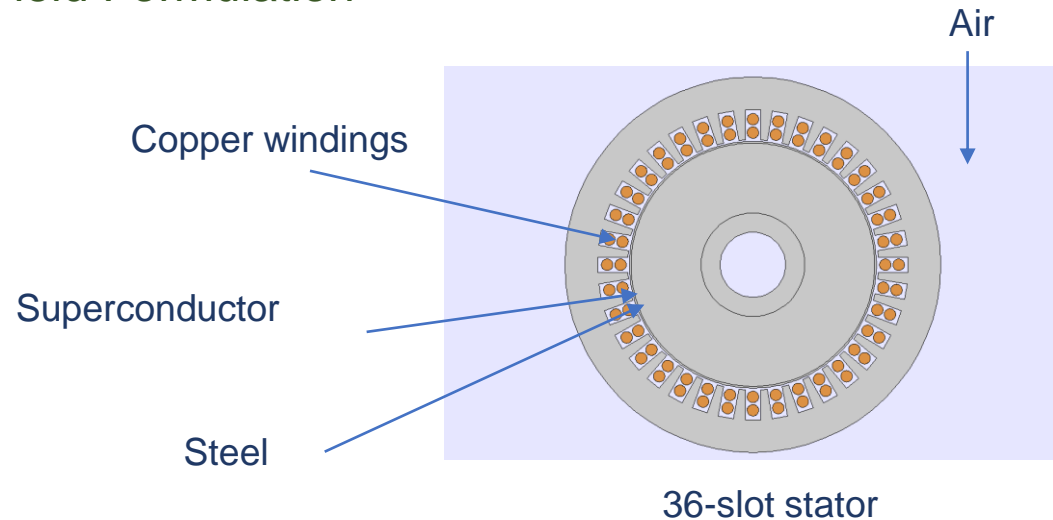
$$E(\mathbf{J}) = E_c \left| \frac{\mathbf{J}}{J_c} \right|^{n-1}$$

J_c Homogeneized

At the boundary, $H_x = H_y = 0$

Linear B-H curve for all materials

Considering Flux-Creep region,
zero field cooling



Simulation Models: A-V Formulation

COMSOL's Rotating Machinery, Magnetics

$$\sigma \frac{\partial A}{\partial t} + \nabla \times H = J_{ext}$$

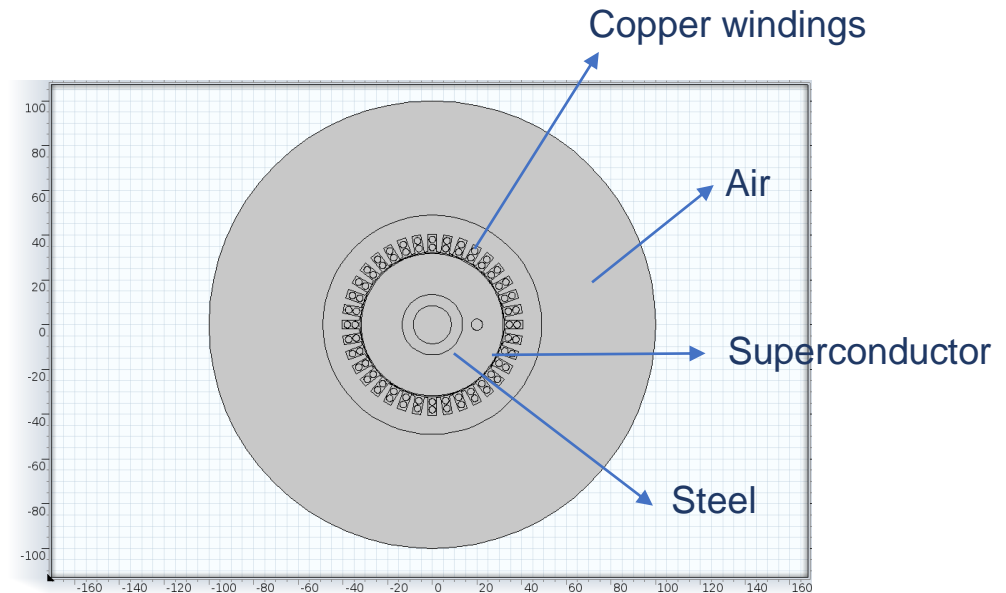
$$B = \nabla \times A$$

$$\nabla \cdot (\mu_0 \mu_r H) = 0$$

$$\sigma = \frac{J_c}{E_c} \left| \frac{E + E_0}{E_c} \right|^{\frac{1-n}{n}}$$

$$J_c(B) = \frac{J_{c0}}{\left(1 + \frac{B_r}{B_0}\right)^\beta} \quad \text{Homogeneized} \quad \text{At the boundary, } A_z = 0$$

Considering Flux-Creep region, zero field cooling



Simulation Models: Mixed Formulation*

COMSOL's General and Coefficient PDEs

$$\sigma \frac{\partial A}{\partial t} - \frac{1}{\mu} \nabla^2 A = J_{ext}$$

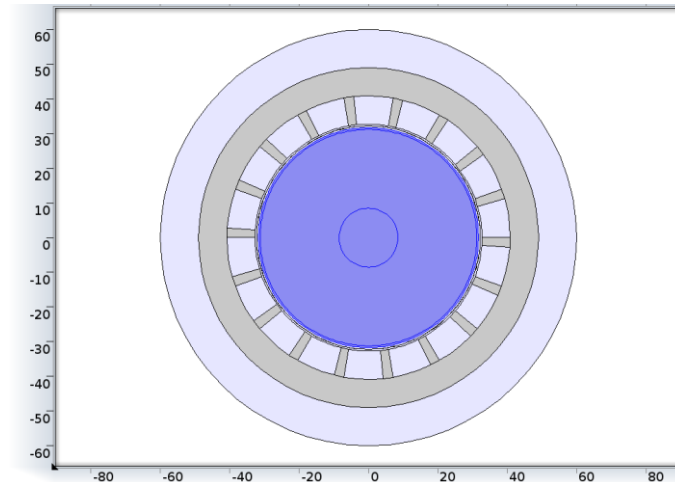
$$B = \nabla \times A$$

$$\frac{\mu \partial H}{\partial t} + \nabla \times E = 0$$

$$\nabla \times H = J$$

Stator,
Rotor air
gap

Rotor



$$H_t^A = H_t^H \quad \rho(J) = \frac{E_c}{J_c} \left| \frac{J}{J_c} \right|^{n-1} \quad J_c \text{ Homogeneized}$$

Considering Flux-Creep region, zero field cooling

*R. Brambilla, F. Grilli, L. Martini, M. Bocchi and G. Angeli. A Finite Element Method Framework for Modeling Rotating Machines With Superconducting Windings. *IEEE Trans. Appl. Supercond.*, vol 28, no 5, Aug. 2018.

Simulation Models: Mixed Formulation*

The mechanical model was implemented with COMSOL's Global ODEs and PDE's and Moving Mesh

$$T_{elect} - T_{mec} = \frac{Jd\omega}{dt}$$

A few remarks:

- A simpler stator was used;
- The stator moves in the opposite direction.

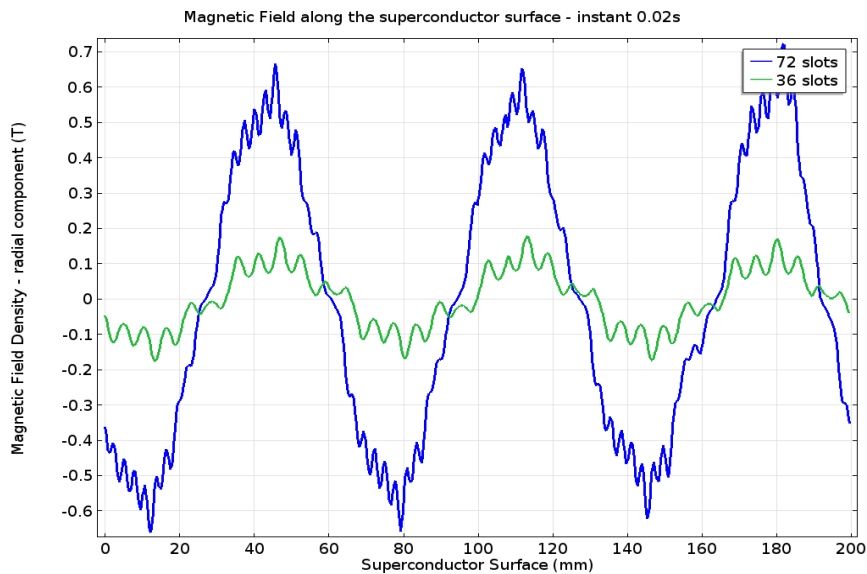
Convergence
Simulation time

Results

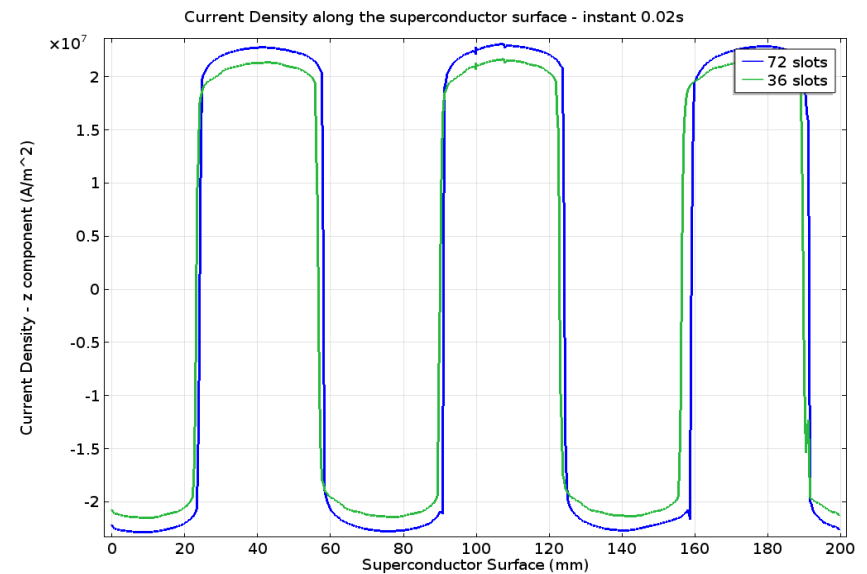
Results: H Formulation Model

$$J_c = 2.98 \times 10^7 \text{ A/m}^2, f = 60\text{Hz}, n=25, \text{ locked rotor}$$

Magnetic Field along the air gap



Induced Current Density – z component along the superconductor ring

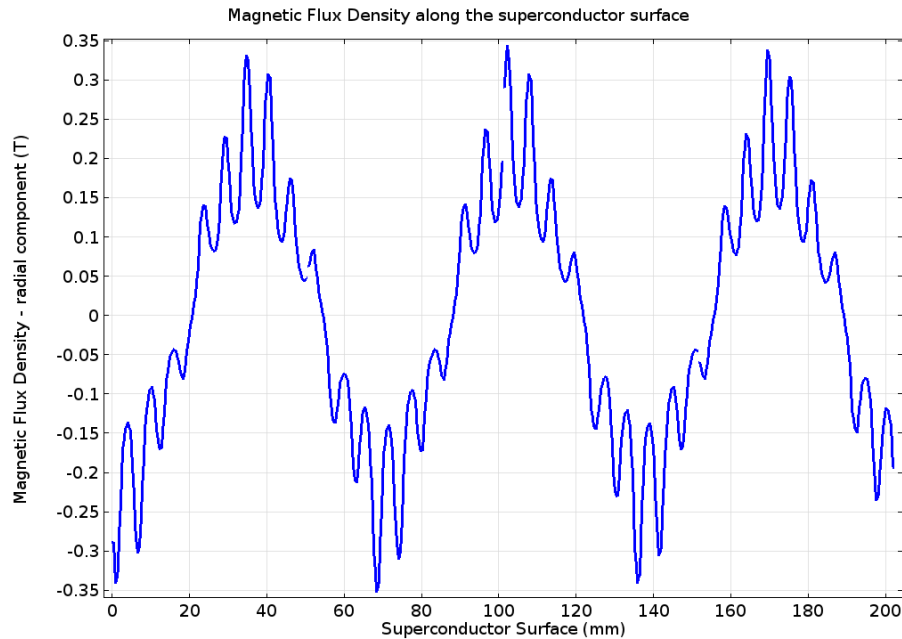


Influence of field harmonics are low in the induced current density

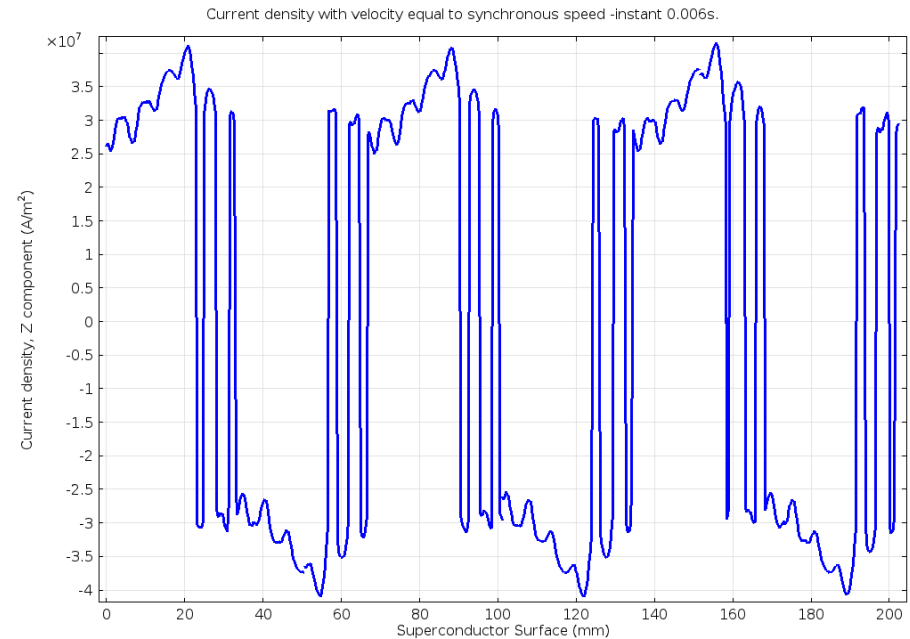
Results: A-V Formulation Model

$$J_{c0} = 2.98 \times 10^7 \text{ A/m}^2, B_0 = 0.5\text{T}, \beta = 1, f = 60\text{Hz}, n=25, \text{ synchronous speed}$$

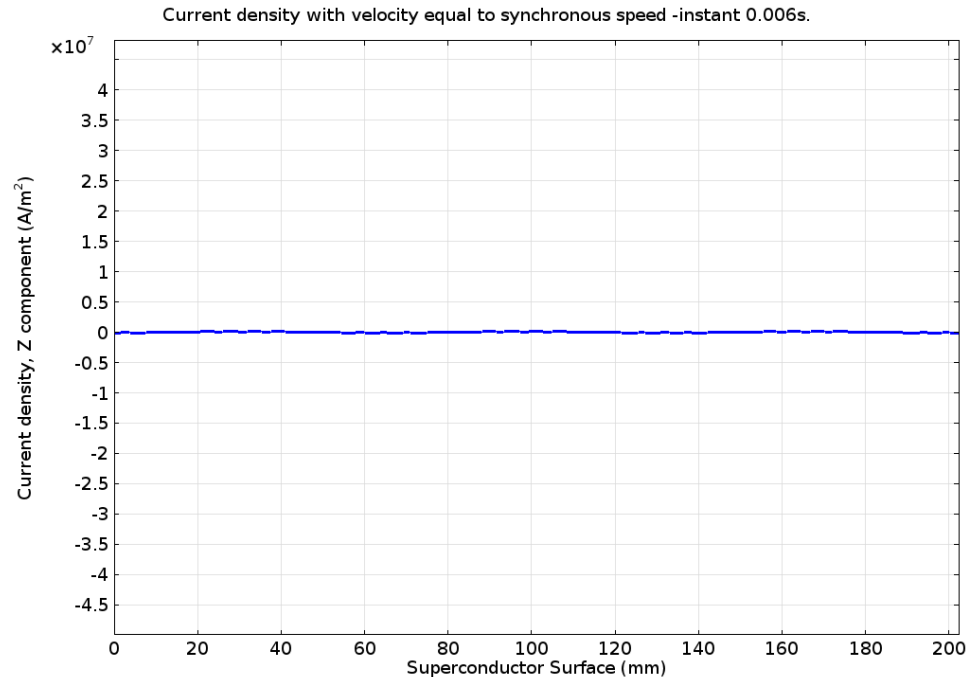
Magnetic Field along the air gap



Induced Current Density along the Superconductor ring



Results: A-V Formulation Model

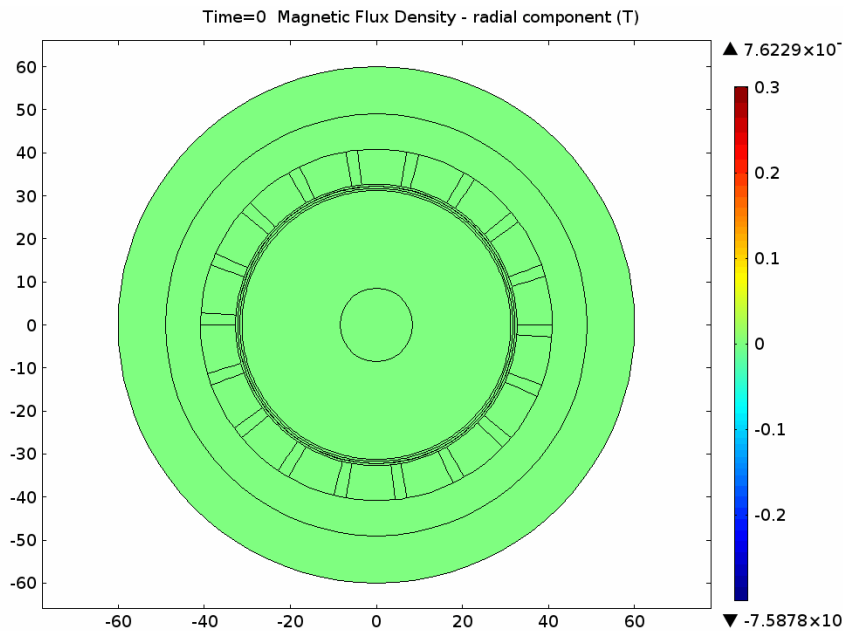


- Many disturbances at synchronous speed, but amplitude stays the same
- Many convergence problems arise

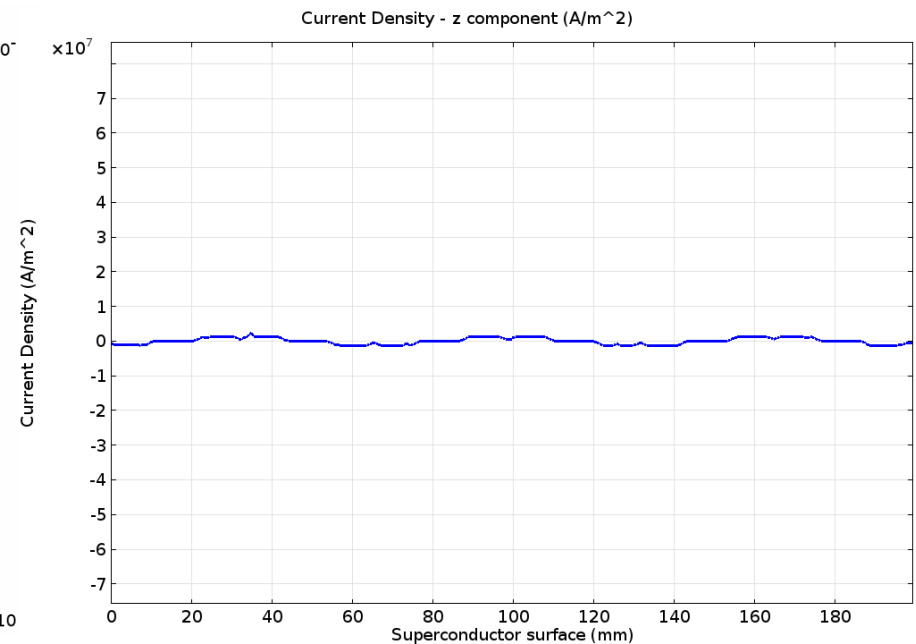
Results: Mixed Formulation Model

$$J_{c0} = 3.437 \times 10^7 \text{ A/m}^2, f = 60\text{Hz}, n=25, \text{ no load condition}$$

Magnetic Field – radial component



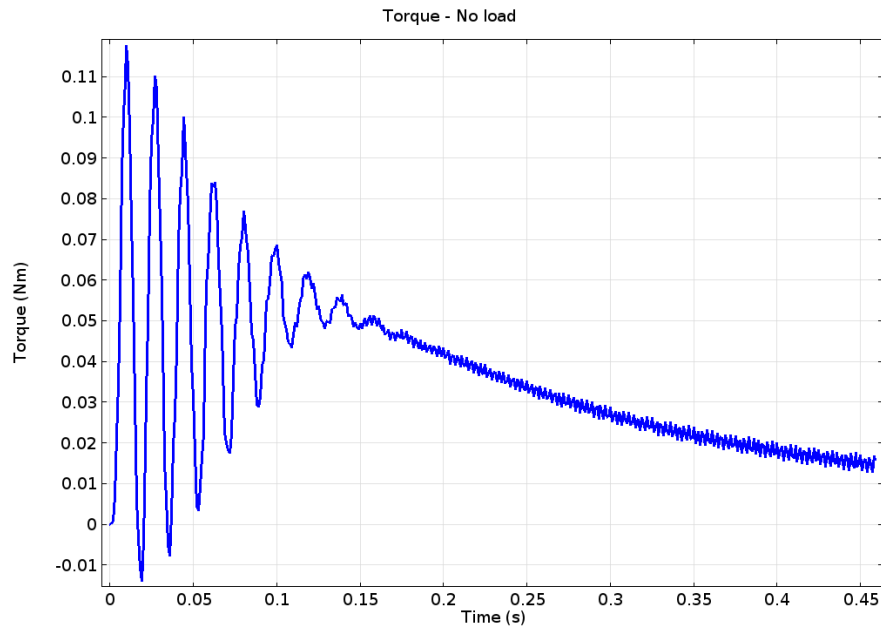
Current Density along the Superconductor ring



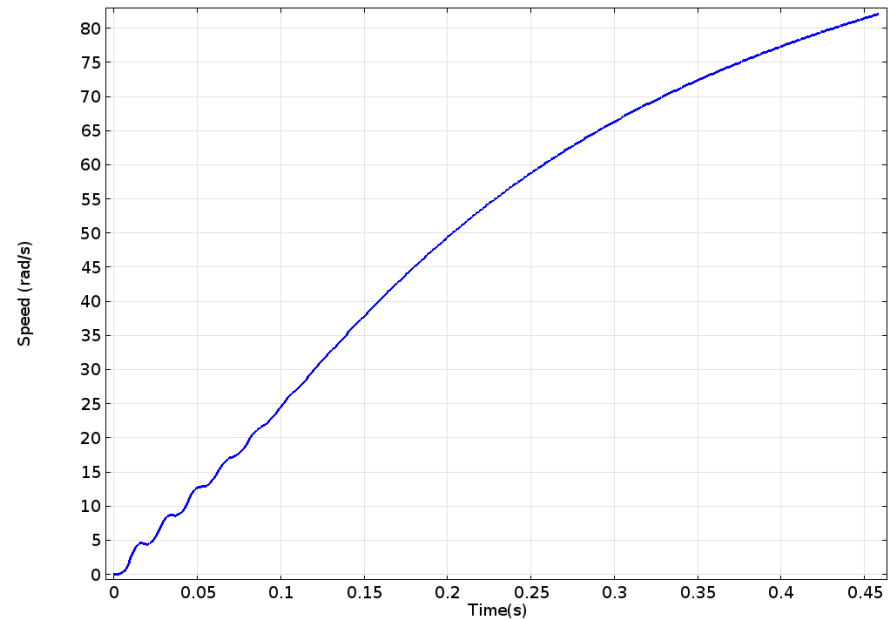
Results: Mixed Formulation Model

$$J_{c0} = 3.437 \times 10^7 \text{ A/m}^2, f = 60\text{Hz}, n=25, \text{ no load condition}$$

Torque vs Time



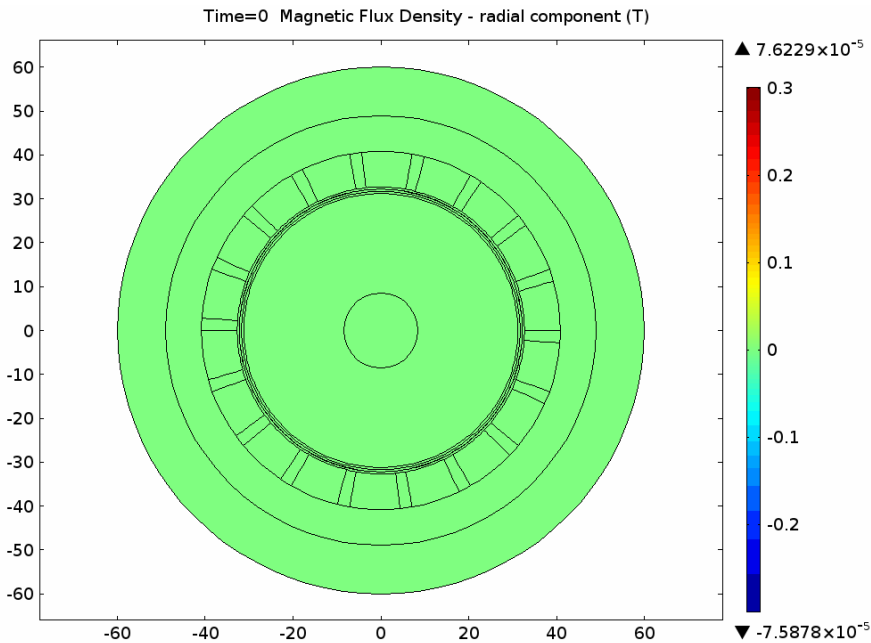
Speed vs Time



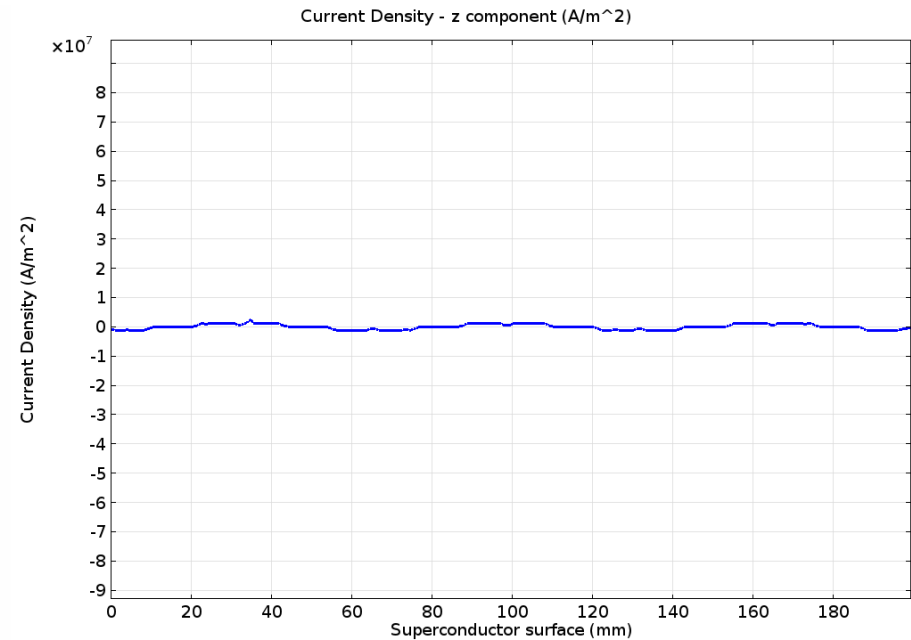
Results: Mixed Formulation Model

$$J_{c0} = 3.437 \times 10^7 \text{ A/m}^2, f = 60\text{Hz}, n=25, \text{ load condition}$$

Magnetic Field – radial component

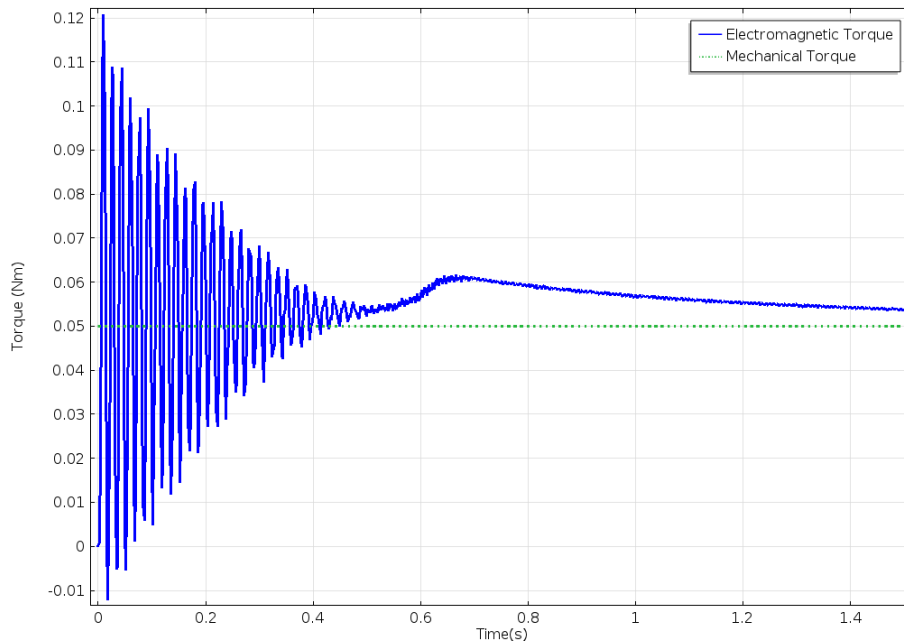


Current Density along the Superconductor ring

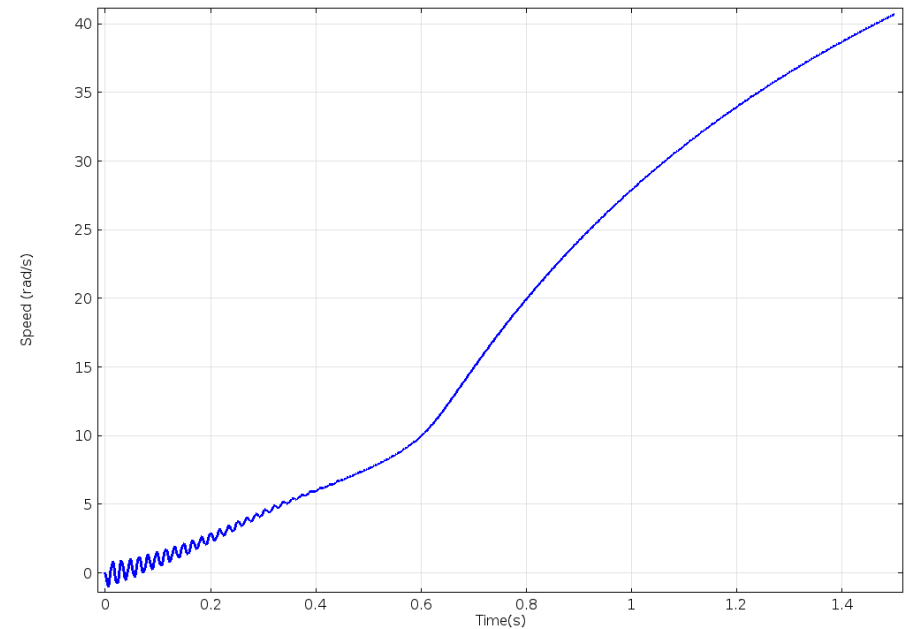


Results: Mixed Formulation Model

Torque vs Time



Speed vs Time



Conclusion

- Air-gap magnetic field harmonics have little impact on the induced current density;
- As speed increases, the current density distribution along the ring increases;
- The hysteresis region is larger than expected;
- The speed response is overdamped.

Thank You!

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Support

